Data Mining – Preprocessing

CS 431 – Advanced Topics in AI

These slides are adapted from J. Han and M. Kamber’s book slides (http://www.cs.sfu.ca/~han)

Why Data Preprocessing?

- Data in the real world is dirty
  - incomplete: lacking attribute values, lacking certain attributes of interest, or containing only aggregate data
  - noisy: containing errors or outliers
  - inconsistent: containing discrepancies in codes or names
- No quality data, no quality mining results!
  - Quality decisions must be based on quality data
- No quality data, inefficient mining process!
  - Complete, noise-free, and consistent data means faster algorithms
Multi-Dimensional Measure of Data Quality

- A well-accepted multidimensional view:
  - Accuracy
  - Completeness
  - Consistency
  - Timeliness
  - Believability
  - Value added
  - Interpretability
  - Accessibility
- Broad categories:
  - intrinsic, contextual, representational, and accessibility.

Major Tasks in Data Preprocessing

- Data cleaning
  - Fill in missing values, smooth noisy data, identify or remove outliers, and resolve inconsistencies
- Data integration
  - Integration of multiple databases, data cubes, or files
- Data transformation
  - Normalization and aggregation
- Data reduction
  - Obtains reduced representation in volume but produces the same or similar analytical results
- Data discretization
  - Part of data reduction but with particular importance, especially for numerical data
Forms of data preprocessing

Data Cleaning
- Fill in missing values
- Identify outliers and smooth out noisy data
- Correct inconsistent data
Missing Data

- Data is not always available
  - E.g., many tuples have no recorded value for several attributes, such as customer income in sales data
- Missing data may be due to
  - equipment malfunction
  - inconsistent with other recorded data and thus deleted
  - data not entered due to misunderstanding
  - certain data may not be considered important at the time of entry
  - not register history or changes of the data
- Missing data may need to be inferred.

How to Handle Missing Data?

- Ignore the tuple: usually done when class label is missing (assuming the tasks in classification—not effective when the percentage of missing values per attribute varies considerably.
- Fill in the missing value manually: tedious + infeasible?
- Use a global constant to fill in the missing value: e.g., “unknown”, a new class?! 
- Use the attribute mean to fill in the missing value
- Use the attribute mean for all samples belonging to the same class to fill in the missing value: smarter
- Use the most probable value to fill in the missing value: inference-based such as Bayesian formula or decision tree
Noisy Data

- Noise: random error or variance in a measured variable
- Incorrect attribute values may be due to
  - faulty data collection instruments
  - data entry problems
  - data transmission problems
  - technology limitation
  - inconsistency in naming convention
- Other data problems which requires data cleaning
  - duplicate records
  - incomplete data
  - inconsistent data

How to Handle Noisy Data?

- Binning method:
  - first sort data and partition into (equi-depth) bins
  - then one can smooth by bin means, smooth by bin median, smooth by bin boundaries, etc.
- Clustering
  - detect and remove outliers
- Combined computer and human inspection
  - detect suspicious values and check by human
- Regression
  - smooth by fitting the data into regression functions
**Simple Discretization Methods: Binning**

- Equal-width (distance) partitioning:
  - It divides the range into \( N \) intervals of equal size:
    uniform grid
  - if \( A \) and \( B \) are the lowest and highest values of the attribute, the width of intervals will be: \( W = (B - A)/N \).
  - The most straightforward
  - But outliers may dominate presentation
  - Skewed data is not handled well.

- Equal-depth (frequency) partitioning:
  - It divides the range into \( N \) intervals, each containing approximately same number of samples
  - Good data scaling
  - Managing categorical attributes can be tricky.

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**Binning Methods for Data Smoothing**

* Sorted data for price (in dollars): 4, 8, 9, 15, 21, 21, 24, 25, 26, 28, 29, 34
* Partition into (equi-depth) bins:
  - Bin 1: 4, 8, 9, 15
  - Bin 2: 21, 21, 24, 25
  - Bin 3: 26, 28, 29, 34
* Smoothing by bin means:
  - Bin 1: 9, 9, 9, 9
  - Bin 2: 23, 23, 23, 23
  - Bin 3: 29, 29, 29, 29
* Smoothing by bin boundaries:
  - Bin 1: 4, 4, 4, 15
  - Bin 2: 21, 21, 25, 25
  - Bin 3: 26, 26, 26, 34
Cluster Analysis

Regression

\[ y = x + 1 \]
Data Integration

- Data integration:
  - combines data from multiple sources into a coherent store
- Schema integration
  - integrate metadata from different sources
  - Entity identification problem: identify real world entities from multiple data sources, e.g., A.cust-id ≡ B.cust-#
- Detecting and resolving data value conflicts
  - for the same real world entity, attribute values from different sources are different
  - possible reasons: different representations, different scales, e.g., metric vs. British units

Handling Redundant Data in Data Integration

- Redundant data occur often when integration of multiple databases
  - The same attribute may have different names in different databases
  - One attribute may be a “derived” attribute in another table, e.g., annual revenue
- Redundant data may be able to be detected by correlational analysis
- Careful integration of the data from multiple sources may help reduce/avoid redundancies and inconsistencies and improve mining speed and quality
Data Transformation

- Smoothing: remove noise from data
- Aggregation: summarization, data cube construction
- Generalization: concept hierarchy climbing
- Normalization: scaled to fall within a small, specified range
  - min-max normalization
  - z-score normalization
  - normalization by decimal scaling
- Attribute/feature construction
  - New attributes constructed from the given ones

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Data Transformation:

Normalization

- min-max normalization
  \[ v' = \frac{v - \text{min}_A}{\text{max}_A - \text{min}_A} \times (\text{new}_A - \text{min}_A) + \text{new}_A \]
- z-score normalization
  \[ v' = \frac{v - \text{mean}_A}{\text{stand}_A \text{ dev}_A} \]
- normalization by decimal scaling
  \[ v' = \frac{v}{10^j} \]
  Where \( j \) is the smallest integer such that \( \text{Max}(|v'|) < 1 \)
Data Reduction Strategies

- Warehouse may store terabytes of data: Complex data analysis/mining may take a very long time to run on the complete data set
- Data reduction
  - Obtains a reduced representation of the data set that is much smaller in volume but yet produces the same (or almost the same) analytical results
- Data reduction strategies
  - Data cube aggregation
  - Dimensionality reduction
  - Numerosity reduction
  - Discretization and concept hierarchy generation

Data Cube Aggregation

- The lowest level of a data cube
  - the aggregated data for an individual entity of interest
  - e.g., a customer in a phone calling data warehouse.
- Multiple levels of aggregation in data cubes
  - Further reduce the size of data to deal with
- Reference appropriate levels
  - Use the smallest representation which is enough to solve the task
- Queries regarding aggregated information should be answered using data cube, when possible
Dimensionality Reduction

- Feature selection (i.e., attribute subset selection):
  - Select a minimum set of features such that the probability distribution of different classes given the values for those features is as close as possible to the original distribution given the values of all features
  - reduce # of patterns in the patterns, easier to understand
- Heuristic methods (due to exponential # of choices):
  - step-wise forward selection
  - step-wise backward elimination
  - combining forward selection and backward elimination
  - decision-tree induction

Example of Decision Tree Induction

Initial attribute set: 
\{A1, A2, A3, A4, A5, A6\}

A4 ?

A1? A6?

Class 1 Class 2 Class 1 Class 2

-----> Reduced attribute set: \{A1, A4, A6\}
Heuristic Feature Selection Methods

- There are $2^d$ possible sub-features of $d$ features
- Several heuristic feature selection methods:
  - Best single features under the feature independence assumption: choose by significance tests.
  - Best step-wise feature selection:
    - The best single-feature is picked first
    - Then next best feature condition to the first, ...
  - Step-wise feature elimination:
    - Repeatedly eliminate the worst feature
  - Best combined feature selection and elimination:
  - Optimal branch and bound:
    - Use feature elimination and backtracking

Data Compression

- String compression
  - There are extensive theories and well-tuned algorithms
  - Typically lossless
  - But only limited manipulation is possible without expansion
- Audio/video compression
  - Typically lossy compression, with progressive refinement
  - Sometimes small fragments of signal can be reconstructed without reconstructing the whole
  - Time sequence is not audio
    - Typically short and vary slowly with time
Data Compression

Original Data

Compressed Data

Original Data

Approximated

lossless

lossy

Wavelet Transforms

- Discrete wavelet transform (DWT): linear signal processing
- Compressed approximation: store only a small fraction of the strongest of the wavelet coefficients
- Similar to discrete Fourier transform (DFT), but better lossy compression, localized in space
- Method:
  - Length, $L$, must be an integer power of 2 (padding with 0s, when necessary)
  - Each transform has 2 functions: smoothing, difference
  - Applies to pairs of data, resulting in two set of data of length $L/2$
  - Applies two functions recursively, until reaches the desired length
Principal Component Analysis

- Given $N$ data vectors from $k$-dimensions, find $c \leq k$ orthogonal vectors that can be best used to represent data
  - The original data set is reduced to one consisting of $N$ data vectors on $c$ principal components (reduced dimensions)
- Each data vector is a linear combination of the $c$ principal component vectors
- Works for numeric data only
- Used when the number of dimensions is large
Numerosity Reduction

- Parametric methods
  - Assume the data fits some model, estimate model parameters, store only the parameters, and discard the data (except possible outliers)
  - Log-linear models: obtain value at a point in m-D space as the product on appropriate marginal subspaces
- Non-parametric methods
  - Do not assume models
  - Major families: histograms, clustering, sampling

Regression and Log-Linear Models

- Linear regression: Data are modeled to fit a straight line
  - Often uses the least-square method to fit the line
- Multiple regression: allows a response variable Y to be modeled as a linear function of multidimensional feature vector
- Log-linear model: approximates discrete multidimensional probability distributions
Regression Analysis and Log-Linear Models

- **Linear regression**: \( Y = \alpha + \beta X \)
  - Two parameters, \( \alpha \) and \( \beta \), specify the line and are to be estimated by using the data at hand.
  - Using the least squares criterion to the known values of \( Y_1, Y_2, \ldots, X_1, X_2, \ldots \).
- **Multiple regression**: \( Y = b_0 + b_1 X_1 + b_2 X_2 \).
  - Many nonlinear functions can be transformed into the above.
- **Log-linear models**:
  - The multi-way table of joint probabilities is approximated by a product of lower-order tables.
  - Probability: \( p(a, b, c, d) = \alpha ab \beta ac \chi ad \delta bcd \)

Histograms

- A popular data reduction technique
- Divide data into buckets and store average (sum) for each bucket
- Can be constructed optimally in one dimension using dynamic programming
- Related to quantization problems.
Clustering

- Partition data set into clusters, and one can store cluster representation only
- Can be very effective if data is clustered but not if data is “smeared”
- Can have hierarchical clustering and be stored in multi-dimensional index tree structures
- There are many choices of clustering definitions and clustering algorithms, further detailed in Chapter 8

Sampling

- Allow a mining algorithm to run in complexity that is potentially sub-linear to the size of the data
- Choose a representative subset of the data
  - Simple random sampling may have very poor performance in the presence of skew
- Develop adaptive sampling methods
  - Stratified sampling:
    - Approximate the percentage of each class (or subpopulation of interest) in the overall database
    - Used in conjunction with skewed data
- Sampling may not reduce database I/Os (page at a time).
Sampling

Raw Data

SRSWOR
(simple random sample without replacement)

SRSWR

Cluster/Stratified Sample

Raw Data
Hierarchical Reduction

- Use multi-resolution structure with different degrees of reduction
- Hierarchical clustering is often performed but tends to define partitions of data sets rather than "clusters"
- Parametric methods are usually not amenable to hierarchical representation
- Hierarchical aggregation
  - An index tree hierarchically divides a data set into partitions by value range of some attributes
  - Each partition can be considered as a bucket
  - Thus an index tree with aggregates stored at each node is a hierarchical histogram

Discretization

- Three types of attributes:
  - Nominal — values from an unordered set
  - Ordinal — values from an ordered set
  - Continuous — real numbers
- Discretization:
  - divide the range of a continuous attribute into intervals
  - Some classification algorithms only accept categorical attributes.
  - Reduce data size by discretization
  - Prepare for further analysis
Discretization and Concept hierarchy

- Discretization
  - reduce the number of values for a given continuous attribute by dividing the range of the attribute into intervals. Interval labels can then be used to replace actual data values.
- Concept hierarchies
  - reduce the data by collecting and replacing low level concepts (such as numeric values for the attribute age) by higher level concepts (such as young, middle-aged, or senior).

Discretization and concept hierarchy generation for numeric data

- Binning (see sections before)
- Histogram analysis (see sections before)
- Clustering analysis (see sections before)
- Entropy-based discretization
- Segmentation by natural partitioning
Entropy-Based Discretization

- Given a set of samples $S$, if $S$ is partitioned into two intervals $S_1$ and $S_2$ using boundary $T$, the entropy after partitioning is
  $$ E(S, T) = \frac{|S_1|}{|S|} Ent(S_1) + \frac{|S_2|}{|S|} Ent(S_2) $$

- The boundary that minimizes the entropy function over all possible boundaries is selected as a binary discretization.

- The process is recursively applied to partitions obtained until some stopping criterion is met, e.g.,
  $$ Ent(S) - E(T, S) > \delta $$

- Experiments show that it may reduce data size and improve classification accuracy

Segmentation by natural partitioning

- 3-4-5 rule can be used to segment numeric data into relatively uniform, “natural” intervals.

  * If an interval covers 3, 6, 7 or 9 distinct values at the most significant digit, partition the range into 3 equi-width intervals.

  * If it covers 2, 4, or 8 distinct values at the most significant digit, partition the range into 4 intervals.

  * If it covers 1, 5, or 10 distinct values at the most significant digit, partition the range into 5 intervals.
Example of 3-4-5 rule

Concept hierarchy generation for categorical data

- Specification of a partial ordering of attributes explicitly at the schema level by users or experts
- Specification of a portion of a hierarchy by explicit data grouping
- Specification of a set of attributes, but not of their partial ordering
- Specification of only a partial set of attributes
Specification of a set of attributes

Concept hierarchy can be automatically generated based on the number of distinct values per attribute in the given attribute set. The attribute with the most distinct values is placed at the lowest level of the hierarchy.

- country
  - province_or_state
    - city
      - street

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Number of Distinct Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>country</td>
<td>15</td>
</tr>
<tr>
<td>province_or_state</td>
<td>65</td>
</tr>
<tr>
<td>city</td>
<td>3567</td>
</tr>
<tr>
<td>street</td>
<td>674,339</td>
</tr>
</tbody>
</table>

Summary

- Data preparation is a big issue for both warehousing and mining
- Data preparation includes
  - Data cleaning and data integration
  - Data reduction and feature selection
  - Discretization
- A lot of methods have been developed but still an active area of research
References